

Package: nnTensor (via r-universe)

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Description Some functions for performing non-negative matrix factorization, non-negative CANDECOMP/PARAFAC (CP) decomposition, non-negative Tucker decomposition, and generating toy model data. See Andrzej Cichock et al (2009) and the reference section of GitHub README.md <<https://github.com/rikenbit/nnTensor>>, for details of the methods.

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URL <https://github.com/rikenbit/nnTensor>

VignetteBuilder knitr

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nnTensor-package	<i>Non-Negative Tensor Decomposition</i>
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Description

Some functions for performing non-negative matrix factorization, non-negative CANDECOMP/PARAFAC (CP) decomposition, non-negative Tucker decomposition, and generating toy model data. See Andrzej Cichock et al (2009) and the reference section of GitHub README.md <<https://github.com/rikenbit/nnTensor>>, for details of the methods.

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References

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- Art B. Owen et. al., (2009). Bi-Cross-Validation of the SVD and the Nonnegative Matrix Factorization. *The Annals of Applied Statistics*

See Also

[toyModel,NMF,NTF,NTD,recTensor,plotTensor3D](#)

Examples

```
ls("package:nnTensor")
```

GabrielNMF	<i>Gabriel-type Bi-Cross-Validation for Non-negative Matrix Factorization</i>
------------	---

Description

The input data is assumed to be non-negative matrix. GabrielNMF divides the input file into four matrices (A, B, C, and D) and perform cross validation by the prediction of A from the matrices B, C, and D.

Usage

```
GabrielNMF(X, J = 3, nx = 5, ny = 5, ...)
```

Arguments

X	The input matrix which has N-rows and M-columns.
J	The number of low-dimension ($J < \{N, M\}$).
nx	The number of hold-out in row-wise direction ($2 < nx < N$).
ny	The number of hold-out in row-wise direction ($2 < ny < M$).
...	Other parameters for NMF function.

Value

TestRecError : The reconstruction error calculated by Gabriel-style Bi-Cross Validation.

Author(s)

Koki Tsuyuzaki

References

Art B. Owen et. al., (2009). Bi-Cross-Validation of the SVD and the Nonnegative Matrix Factorization. *The Annals of Applied Statistics*

Examples

```
if(interactive()){
  # Test data
  matdata <- toyModel(model = "NMF")

  # Bi-Cross-Validation
  BCV <- rep(0, length=5)
  names(BCV) <- 2:6
  for(j in seq(BCV)){
    print(j+1)
    BCV[j] <- mean(GabrielNMF(matdata, J=j+1, nx=2, ny=2)$TestRecError)
  }
}
```

```

proper.rank <- as.numeric(names(BCV)[which(BCV == min(BCV))])

# NMF
out <- NMF(matdata, J=proper.rank)
}

```

jNMF

*Joint Non-negative Matrix Factorization Algorithms (jNMF)***Description**

The input data objects are assumed to be non-negative matrices. jNMF decompose the matrices to two low-dimensional factor matrices simultaneously.

Usage

```

jNMF(X, M=NULL, pseudocount=.Machine$double.eps,
      initW=NULL, initV=NULL, initH=NULL, fixW=FALSE, fixV=FALSE,
      fixH=FALSE,
      L1_W=1e-10, L1_V=1e-10, L1_H=1e-10,
      L2_W=1e-10, L2_V=1e-10, L2_H=1e-10,
      J = 3, w=NULL, algorithm = c("Frobenius", "KL", "IS", "PLTF"),
      p=1, thr = 1e-10, num.iter = 100, viz = FALSE,
      figdir = NULL, verbose = FALSE)

```

Arguments

X	A list containing input matrices (X_k , $\langle N \times M_k \rangle$, $k=1..K$).
M	A list containing the mask matrices (X_k , $\langle N \times M_k \rangle$, $k=1..K$). If the input matrix has missing values, specify the element as 0 (otherwise 1).
pseudocount	The pseudo count to avoid zero division, when the element is zero (Default: Machine Epsilon).
initW	The initial values of factor matrix W, which has N-rows and J-columns (Default: NULL).
initV	A list containing the initial values of multiple factor matrices (V_k , $\langle N \times J \rangle$, $k=1..K$, Default: NULL).
initH	A list containing the initial values of multiple factor matrices (H_k , $\langle M_k \times J \rangle$, $k=1..K$, Default: NULL).
fixW	Whether the factor matrix W is updated in each iteration step (Default: FALSE).
fixV	Whether the factor matrices V_k are updated in each iteration step (Default: FALSE).
fixH	Whether the factor matrices H_k are updated in each iteration step (Default: FALSE).
L1_W	Parameter for L1 regularization (Default: 1e-10). This also works as small positive constant to prevent division by zero, so should be set as 0.

L1_V	Paramter for L1 regularitation (Default: 1e-10). This also works as small positive constant to prevent division by zero, so should be set as 0.
L1_H	Paramter for L1 regularitation (Default: 1e-10). This also works as small positive constant to prevent division by zero, so should be set as 0.
L2_W	Paramter for L2 regularitation (Default: 1e-10).
L2_V	Paramter for L2 regularitation (Default: 1e-10).
L2_H	Paramter for L2 regularitation (Default: 1e-10).
J	Number of low-dimension ($J < N, M_k$).
w	Weight vector (Default: NULL)
algorithm	Divergence between X and \bar{X} . "Frobenius", "KL", and "IS" are available (Default: "KL").
p	The parameter of Probabilistic Latent Tensor Factorization (p=0: Frobenius, p=1: KL, p=2: IS)
thr	When error change rate is lower than thr, the iteration is terminated (Default: 1E-10).
num.iter	The number of interation step (Default: 100).
viz	If viz == TRUE, internal reconstructed matrix can be visualized.
figdir	the directory for saving the figure, when viz == TRUE.
verbose	If verbose == TRUE, Error change rate is generated in console windos.

Value

W : A matrix which has N-rows and J-columns ($J < N, M_k$). V : A list which has multiple elements containing N-rows and J-columns ($J < N, M_k$). H : A list which has multiple elements containing M_k -rows and J-columns matrix ($J < N, M_k$). RecError : The reconstruction error between data matrix and reconstructed matrix from W and H. TrainRecError : The reconstruction error calculated by training set (observed values specified by M). TestRecError : The reconstruction error calculated by test set (missing values specified by M). RelChange : The relative change of the error.

Author(s)

Koki Tsuyuzaki

References

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- N. Fujita et al., (2018) Biomarker discovery by integrated joint non-negative matrix factorization and pathway signature analyses, *Scientific Report*

Examples

```
matdata <- toyModel(model = "siNMF_Hard")
out <- jNMF(matdata, J=2, num.iter=2)
```

kFoldMaskTensor	<i>Mask tensors generator to perform k-fold cross validation</i>
-----------------	--

Description

The output multiple mask tensors can be immediately specified as the argument `M` for `NTF()` or `NTD()`.

Usage

```
kFoldMaskTensor(X, k=3, seeds=123, sym=FALSE)
```

Arguments

<code>X</code>	An <code>rTensor</code> object.
<code>k</code>	Number of split for k-fold cross validation (Default: 3).
<code>seeds</code>	Random seed to use for <code>set.seed()</code> (Default: 123).
<code>sym</code>	Data will be dropped symmetrically (available only when matrix is specified, Default: FALSE).

Author(s)

Koki Tsuyuzaki

Examples

```
tensordata <- toyModel(model = "CP")
str(kFoldMaskTensor(tensordata, k=5))
```

Description

The input data is assumed to be non-negative matrix. NMF decompose the matrix to two low-dimensional factor matrices. This function is also used as initialization step of tensor decomposition (see also NTF and NTD).

Usage

```
NMF(X, M=NULL, pseudocount=.Machine$double.eps, initU=NULL, initV=NULL,
    fixU=FALSE, fixV=FALSE,
    L1_U=1e-10, L1_V=1e-10, L2_U=1e-10, L2_V=1e-10, J = 3,
    rank.method=c("all", "ccc", "dispersion", "rss", "evar", "residuals",
    "sparseness.basis", "sparseness.coef", "sparseness2.basis",
    "sparseness2.coef", "norm.info.gain.basis", "norm.info.gain.coef",
    "singular", "volume", "condition"), runtime=30,
    algorithm = c("Frobenius", "KL", "IS", "Pearson", "Hellinger", "Neyman",
    "Alpha", "Beta", "ALS", "PGD", "HALS", "GCD", "Projected", "NHR", "DTPP",
    "Orthogonal", "OrthReg"), Alpha = 1, Beta = 2,
    eta = 1e-04, thr1 = 1e-10, thr2 = 1e-10, tol = 1e-04,
    num.iter = 100, viz = FALSE, figdir = NULL, verbose = FALSE)
```

Arguments

X	The input matrix which has N-rows and M-columns.
M	The mask matrix which has N-rows and M-columns. If the input matrix has missing values, specify the elements as 0 (otherwise 1).
pseudocount	The pseudo count to avoid zero division, when the element is zero (Default: Machine Epsilon).
initU	The initial values of factor matrix U, which has N-rows and J-columns (Default: NULL).
initV	The initial values of factor matrix V, which has M-rows and J-columns (Default: NULL).
fixU	Whether the factor matrix U is updated in each iteration step (Default: FALSE).
fixV	Whether the factor matrix V is updated in each iteration step (Default: FALSE).
L1_U	Paramter for L1 regularitation (Default: 1e-10). This also works as small positive constant to prevent division by zero, so should be set as 0.
L1_V	Paramter for L1 regularitation (Default: 1e-10). This also works as small positive constant to prevent division by zero, so should be set as 0.
L2_U	Paramter for L2 regularitation (Default: 1e-10).
L2_V	Paramter for L2 regularitation (Default: 1e-10).

J	The number of low-dimension ($J < \{N, M\}$). If a numerical vector is specified (e.g. 2:6), the appropriate rank is estimated.
rank.method	The rank estimation method (Default: "all"). Only if the J option is specified as a numerical vector longer than two, this option will be active.
runtime	The number of trials to estimate rank (Default: 10).
algorithm	NMF algorithms. "Frobenius", "KL", "IS", "Pearson", "Hellinger", "Neyman", "Alpha", "Beta", "ALS", "PGD", "HALS", "GCD", "Projected", "NHR", "DTPP", "Orthogonal", and "OrthReg" are available (Default: "Frobenius").
Alpha	The parameter of Alpha-divergence.
Beta	The parameter of Beta-divergence.
eta	The stepsize for PGD algorithm (Default: 0.0001).
thr1	When error change rate is lower than thr1, the iteration is terminated (Default: 1E-10).
thr2	If the minus-value is generated, replaced as thr2 (Default: 1E-10). This value is used within the internal function .positive().
tol	The tolerance parameter used in GCD algorithm.
num.iter	The number of iteration step (Default: 100).
viz	If viz == TRUE, internal reconstructed matrix can be visualized.
figdir	The directory for saving the figure, when viz == TRUE.
verbose	If verbose == TRUE, Error change rate is generated in console window.

Value

U : A matrix which has N-rows and J-columns ($J < \{N, M\}$). V : A matrix which has M-rows and J-columns ($J < \{N, M\}$). J : The number of dimension ($J < \{N, M\}$). RecError : The reconstruction error between data tensor and reconstructed tensor from U and V. TrainRecError : The reconstruction error calculated by training set (observed values specified by M). TestRecError : The reconstruction error calculated by test set (missing values specified by M). RelChange : The relative change of the error. Trial : All the results of the trials to estimate the rank. Runtime : The number of the trials to estimate the rank. RankMethod : The rank estimation method.

Author(s)

Koki Tsuyuzaki

References

- Andrzej CICHOCK, et. al., (2009). Nonnegative Matrix and Tensor Factorizations. *John Wiley & Sons, Ltd*
- Keigo Kimura, (2017). A Study on Efficient Algorithms for Nonnegative Matrix/ Tensor Factorization. *Hokkaido University Collection of Scholarly and Academic Papers*

Examples

```

if(interactive()){
  # Test data
  matdata <- toyModel(model = "NMF")

  # Simple usage
  out <- NMF(matdata, J=5)

  # Rank estimation mode (single method)
  out2 <- NMF(matdata, J=2:10, rank.method="ccc", runtime=3)
  plot(out2)

  # Rank estimation mode (all method)
  out3 <- NMF(matdata, J=2:10, rank.method="all", runtime=10)
  plot(out3)
}

```

NMTF

Non-negative Matrix Tri-Factorization Algorithms (NMTF)

Description

The input data is assumed to be non-negative matrix. NMTF decompose the matrix to three low-dimensional factor matrices.

Usage

```

NMTF(X, M=NULL, pseudocount=.Machine$double.eps,
      initU=NULL, initS=NULL, initV=NULL,
      fixU=FALSE, fixS=FALSE, fixV=FALSE,
      L1_U=1e-10, L1_S=1e-10, L1_V=1e-10,
      L2_U=1e-10, L2_S=1e-10, L2_V=1e-10,
      orthU=FALSE, orthV=FALSE,
      rank = c(3, 4),
      algorithm = c("Frobenius", "KL", "IS", "ALS", "PG", "COD", "Beta"),
      Beta = 2, root = FALSE, thr = 1e-10, num.iter = 100,
      viz = FALSE, figdir = NULL, verbose = FALSE)

```

Arguments

X	The input matrix which has N-rows and M-columns.
M	The mask matrix which has N-rows and M-columns. If the input matrix has missing values, specify the elements as 0 (otherwise 1).
pseudocount	The pseudo count to avoid zero division, when the element is zero (Default: Machine Epsilon).
initU	The initial values of factor matrix U, which has N-rows and J1-columns (Default: NULL).

<code>initS</code>	The initial values of factor matrix S , which has $J1$ -rows and $J2$ -columns (Default: NULL).
<code>initV</code>	The initial values of factor matrix V , which has M -rows and $J2$ -columns (Default: NULL).
<code>fixU</code>	Whether the factor matrix U is updated in each iteration step (Default: FALSE).
<code>fixS</code>	Whether the factor matrix S is updated in each iteration step (Default: FALSE).
<code>fixV</code>	Whether the factor matrix V is updated in each iteration step (Default: FALSE).
<code>L1_U</code>	Paramter for L1 regularitation (Default: 1e-10).
<code>L1_S</code>	Paramter for L1 regularitation (Default: 1e-10).
<code>L1_V</code>	Paramter for L1 regularitation (Default: 1e-10).
<code>L2_U</code>	Paramter for L2 regularitation (Default: 1e-10).
<code>L2_S</code>	Paramter for L2 regularitation (Default: 1e-10).
<code>L2_V</code>	Paramter for L2 regularitation (Default: 1e-10).
<code>orthU</code>	Whether the column vectors of matrix U are orthogonalized (Default: FALSE).
<code>orthV</code>	Whether the column vectors of matrix V are orthogonalized (Default: FALSE).
<code>rank</code>	The number of low-dimension ($J1 < N$ and $J2 < M$) (Default: c(3,4)).
<code>algorithm</code>	NMTF algorithms. "Frobenius", "KL", "IS", "ALS", "PG", "COD", and "Beta" are available (Default: "Frobenius").
<code>Beta</code>	The parameter of Beta-divergence (Default: 2, which means "Frobenius").
<code>root</code>	Whether square root is calculated in each iteration (Default: FALSE).
<code>thr</code>	When error change rate is lower than <code>thr</code> , the iteration is terminated (Default: 1E-10).
<code>num.iter</code>	The number of interation step (Default: 100).
<code>viz</code>	If <code>viz == TRUE</code> , internal reconstructed matrix can be visualized.
<code>figdir</code>	The directory for saving the figure, when <code>viz == TRUE</code> .
<code>verbose</code>	If <code>verbose == TRUE</code> , Error change rate is generated in console window.

Value

U : A matrix which has N -rows and $J1$ -columns ($J1 < N$). S : A matrix which has $J1$ -rows and $J2$ -columns. V : A matrix which has M -rows and $J2$ -columns ($J2 < M$). `rank` : The number of low-dimension ($J1 < N$ and $J2 < M$). `RecError` : The reconstruction error between data tensor and reconstructed tensor from U and V . `TrainRecError` : The reconstruction error calculated by training set (observed values specified by M). `TestRecError` : The reconstruction error calculated by test set (missing values specified by M). `RelChange` : The relative change of the error. `algorithm`: algorithm specified.

Author(s)

Koki Tsuyuzaki

References

- Fast Optimization of Non-Negative Matrix Tri-Factorization: Supporting Information, Andrej Copar, et. al., *PLOS ONE*, 14(6), e0217994, 2019
- Co-clustering by Block Value Decomposition, Bo Long et al., *SIGKDD'05*, 2005
- Orthogonal Nonnegative Matrix Tri-Factorizations for Clustering, Chris Ding et. al., *12th ACM SIGKDD*, 2006

Examples

```
if(interactive()){
  # Test data
  matdata <- toyModel(model = "NMF")

  # Simple usage
  out <- NMTF(matdata, rank=c(4,4))
}
```

 NTD

Non-negative Tucker Decomposition Algorithms (NTD)

Description

The input data is assumed to be non-negative tensor. NTD decompose the tensor to the dense core tensor (S) and low-dimensional factor matrices (A).

Usage

```
NTD(X, M=NULL, pseudocount=.Machine$double.eps, initS=NULL, initA=NULL,
    fixS=FALSE, fixA=FALSE, L1_A=1e-10, L2_A=1e-10,
    rank = rep(3, length=length(dim(X))),
    modes = seq_along(dim(X)),
    algorithm = c("Frobenius", "KL", "IS", "Pearson", "Hellinger", "Neyman",
                  "HALS", "Alpha", "Beta", "NMF"), init = c("NMF", "ALS", "Random"),
    nmf.algorithm = c("Frobenius", "KL", "IS", "Pearson", "Hellinger", "Neyman",
                      "Alpha", "Beta", "ALS", "PGD", "HALS", "GCD", "Projected", "NHR", "DTPP",
                      "Orthogonal", "OrthReg"),
    Alpha = 1,
    Beta = 2, thr = 1e-10, num.iter = 100, num.iter2 = 10, viz = FALSE,
    figdir = NULL, verbose = FALSE)
```

Arguments

- | | |
|---|--|
| X | K-order input tensor which has I_1, I_2, \dots , and I_K dimensions. |
| M | K-order mask tensor which has I_1, I_2, \dots , and I_K dimensions. If the mask tensor has missing values, specify the element as 0 (otherwise 1). |

pseudocount	The pseudo count to avoid zero division, when the element is zero (Default: Machine Epsilon).
initS	The initial values of core tensor which has $I_1, I_2, \dots,$ and I_K dimensions (Default: NULL).
initA	A list containing the initial values of K factor matrices ($A_k, \langle I_k * J_k \rangle, k=1..K$, Default: NULL).
fixS	Whether the core tensor S is updated in each iteration step (Default: FALSE).
fixA	Whether the factor matrices A_k are updated in each iteration step (Default: FALSE).
L1_A	Paramter for L1 regularitation (Default: $1e-10$). This also works as small positive constant to prevent division by zero, so should be set as 0.
L2_A	Paramter for L2 regularitation (Default: $1e-10$).
rank	The number of low-dimension in each mode (Default: 3 for each mode).
modes	The vector of the modes on which to perform the decomposition (Default: $1:K$ <all modes>).
algorithm	NTD algorithms. "Frobenius", "KL", "IS", "Pearson", "Hellinger", "Neyman", "HALS", "Alpha", "Beta", "NMF" are available (Default: "Frobenius").
nmf.algorithm	NMF algorithms, when the algorithm is "NMF". "Frobenius", "KL", "IS", "Pearson", "Hellinger", "Neyman", "Alpha", "Beta", "ALS", "PGD", "HALS", "GCD", "Projected", "NHR", "DTPP", "Orthogonal", and "OrthReg" are available (Default: "Frobenius").
init	The initialization algorithms. "NMF", "ALS", and "Random" are available (Default: "NMF").
Alpha	The parameter of Alpha-divergence.
Beta	The parameter of Beta-divergence.
thr	When error change rate is lower than thr1, the iteration is terminated (Default: $1E-10$).
num.iter	The number of interation step (Default: 100).
num.iter2	The number of NMF interation step, when the algorithm is "NMF" (Default: 10).
viz	If viz == TRUE, internal reconstructed tensor can be visualized.
figdir	the directory for saving the figure, when viz == TRUE (Default: NULL).
verbose	If verbose == TRUE, Error change rate is generated in console windos.

Value

S : K -order tensor object, which is defined as S4 class of rTensor package. A : A list containing K factor matrices. RecError : The reconstruction error between data tensor and reconstructed tensor from S and A . TrainRecError : The reconstruction error calculated by training set (observed values specified by M). TestRecError : The reconstruction error calculated by test set (missing values specified by M). RelChange : The relative change of the error.

Author(s)

Koki Tsuyuzaki

References

Yong-Deok Kim et. al., (2007). Nonnegative Tucker Decomposition. *IEEE Conference on Computer Vision and Pattern Recognition*

Yong-Deok Kim et. al., (2008). Nonnegative Tucker Decomposition With Alpha-Divergence. *IEEE International Conference on Acoustics, Speech and Signal Processing*

Anh Huy Phan, (2008). Fast and efficient algorithms for nonnegative Tucker decomposition. *Advances in Neural Networks - ISNN2008*

Anh Hyu Phan et. al. (2011). Extended HALS algorithm for nonnegative Tucker decomposition and its applications for multiway analysis and classification. *Neurocomputing*

See Also

[plotTensor3D](#)

Examples

```
tensordata <- toyModel(model = "Tucker")
out <- NTF(tensordata, rank=c(2,2,2), algorithm="Frobenius",
  init="Random", num.iter=2)
```

NTF

Non-negative CP Decomposition Algorithms (NTF)

Description

The input data is assumed to be non-negative tensor. NTF decompose the tensor to the diagonal core tensor (S) and low-dimensional factor matrices (A).

Usage

```
NTF(X, M=NULL, pseudocount=.Machine$double.eps, initA=NULL,
  fixA=FALSE, L1_A=1e-10, L2_A=1e-10, rank = 3,
  algorithm = c("Frobenius", "KL", "IS", "Pearson", "Hellinger", "Neyman",
    "HALS", "Alpha-HALS", "Beta-HALS", "Alpha", "Beta"),
  init = c("NMF", "ABS-SVD", "ALS", "Random"), Alpha = 1,
  Beta = 2, thr = 1e-10, num.iter = 100, viz = FALSE,
  figdir = NULL, verbose = FALSE)
```

Arguments

X	K-order input tensor which has $I_1, I_2, \dots,$ and I_K dimensions.
M	K-order mask tensor which has $I_1, I_2, \dots,$ and I_K dimensions. If the mask tensor has missing values, specify the element as 0 (otherwise 1).
pseudocount	The pseudo count to avoid zero division, when the element is zero (Default: Machine Epsilon).
initA	A list containing the initial values of K factor matrices ($A_k, \langle I_k \times J_k \rangle, k=1..K,$ Default: NULL).
fixA	Whether the factor matrices A_k are updated in each iteration step (Default: FALSE).
L1_A	Parameter for L1 regularization (Default: $1e-10$). This also works as small positive constant to prevent division by zero, so should be set as 0.
L2_A	Parameter for L2 regularization (Default: $1e-10$).
rank	The number of low-dimension in each mode (Default: 3).
algorithm	NTF algorithms. "Frobenius", "KL", "IS", "Pearson", "Hellinger", "Neyman", "HALS", "Alpha-HALS", "Beta-HALS", "Alpha", and "Beta" are available (Default: "Frobenius").
init	The initialization algorithms. "NMF", "ABS-SVD", "ALS", and "Random" are available (Default: "NMF").
Alpha	The parameter of Alpha-divergence.
Beta	The parameter of Beta-divergence.
thr	When error change rate is lower than thr1, the iteration is terminated (Default: $1E-10$).
num.iter	The number of iteration step (Default: 100).
viz	If viz == TRUE, internal reconstructed tensor can be visualized.
figdir	the directory for saving the figure, when viz == TRUE (Default: NULL).
verbose	If verbose == TRUE, Error change rate is generated in console windows.

Value

S : K-order tensor object, which is defined as S4 class of rTensor package. A : A list containing K factor matrices. RecError : The reconstruction error between data tensor and reconstructed tensor from S and A. TrainRecError : The reconstruction error calculated by training set (observed values specified by M). TestRecError : The reconstruction error calculated by test set (missing values specified by M). RelChange : The relative change of the error.

Author(s)

Koki Tsuyuzaki

References

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- Anh Huy PHAN et. al., (2008). Multi-way Nonnegative Tensor Factorization Using Fast Hierarchical Alternating Least Squares Algorithm (HALS). *NOLTA2008*
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See Also

[plotTensor3D](#)

Examples

```
tensordata <- toyModel(model = "CP")
out <- NTF(tensordata, rank=3, algorithm="Beta-HALS", num.iter=2)
```

plot.NMF

Plot function of the result of NMF function

Description

Only if J is specified as a vector longer than 1, this function will be active.

Author(s)

Koki Tsuyuzaki

References

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Patrik O. Hoyer (2004). Non-negative Matrix Factorization with Sparseness Constraints. *Journal of Machine Learning* 5

Examples

```
methods(class = "NMF")
```

plotTensor2D	<i>Plot function for visualization of matrix data structure</i>
--------------	---

Description

Combined with recTensor function and the result of NTF or NTD, the reconstructed tensor structure can be visullized.

Usage

```
plotTensor2D(X = NULL, method=c("sd", "mad"),  
            sign=c("positive", "negative", "both"), thr=2)
```

Arguments

X	Matrix object.
method	Cutoff method to focus on large/small value in the tensor data (Default: "sd").
sign	Direction to cutoff the large/small value in the tensor data (Default: "positive").
thr	Threshold of cutoff method (Default: 2).

Author(s)

Koki Tsuyuzaki

Examples

```
tensordata <- toyModel(model = "CP")  
  
out <- NTF(tensordata, rank=3, num.iter=2)  
  
tmp <- tempdir()  
  
png(filename=paste0(tmp, "/NTF.png"))  
plotTensor2D(out$A[[1]])  
dev.off()
```

plotTensor3D *Plot function for visualization of tensor data structure*

Description

Combined with recTensor function and the result of NTF or NTD, the reconstructed tensor structure can be visullized.

Usage

```
plotTensor3D(X = NULL, method=c("sd", "mad"),
  sign=c("positive", "negative", "both"), thr=2)
```

Arguments

X	Tensor object, which is defined as S4 class of rTensor package.
method	Cutoff method to focus on large/small value in the tensor data (Default: "sd").
sign	Direction to cutoff the large/small value in the tensor data (Default: "positive").
thr	Threshold of cutoff method (Default: 2).

Author(s)

Koki Tsuyuzaki

Examples

```
tensordata <- toyModel(model = "CP")

out <- NTF(tensordata, rank=3, algorithm="Beta-HALS", num.iter=2)

tmp <- tempdir()

png(filename=paste0(tmp, "/NTF.png"))
plotTensor3D(recTensor(out$S, out$A))
dev.off()
```

recTensor *Tensor Reconstruction from core tensor (S) and factor matrices (A)*

Description

Combined with plotTensor3D function and the result of NTF or NTD, the reconstructed tesor struc-
ture can be visullized.

Usage

```
recTensor(S = NULL, A = NULL, idx = seq_along(dim(S)), reverse = FALSE)
```

Arguments

S	K-order tensor object, which is defined as S4 class of rTensor package.
A	A list containing K factor matrices.
idx	The direction of mode-n multiplication (Default: 1:K). For example idx=1 is defined. $S \times_1 A$ is calculated (\times_1 : mode-1 multiplication).
reverse	If reverse = TRUE, $t(A[[n]])$ is multiplied to S (Default: FALSE).

Value

Tensor object, which is defined as S4 class of rTensor package.

Author(s)

Koki Tsuyuzaki

See Also

[Tensor-class](#), [NTF](#), [NTD](#)

Examples

```
tensordata <- toyModel(model = "CP")
out <- NTF(tensordata, rank=3, algorithm="Beta-HALS", num.iter=2)
rec <- recTensor(out$S, out$A)
```

 siNMF

Simultaneous Non-negative Matrix Factorization Algorithms (siNMF)

Description

The input data objects are assumed to be non-negative matrices. siNMF decompose the matrices to two low-dimensional factor matrices simultaneously.

Usage

```
siNMF(X, M=NULL, pseudocount=.Machine$double.eps, initW=NULL, initH=NULL,
      fixW=FALSE, fixH=FALSE,
      L1_W=1e-10, L1_H=1e-10, L2_W=1e-10, L2_H=1e-10, J = 3,
      w=NULL, algorithm = c("Frobenius", "KL", "IS", "PLTF"), p=1,
      thr = 1e-10, num.iter = 100,
      viz = FALSE, figdir = NULL, verbose = FALSE)
```

Arguments

X	A list containing the input matrices (X_k , $\langle N \times M_k \rangle$, $k=1..K$).
M	A list containing the mask matrices (X_k , $\langle N \times M_k \rangle$, $k=1..K$). If the input matrix has missing values, specify the element as 0 (otherwise 1).
pseudocount	The pseudo count to avoid zero division, when the element is zero (Default: Machine Epsilon).
initW	The initial values of factor matrix W, which has N-rows and J-columns (Default: NULL).
initH	A list containing the initial values of multiple factor matrices (H_k , $\langle M_k \times J \rangle$, $k=1..K$, Default: NULL).
fixW	Whether the factor matrix W is updated in each iteration step (Default: FALSE).
fixH	Whether the factor matrices H_k are updated in each iteration step (Default: FALSE).
L1_W	Parameter for L1 regularization (Default: 1e-10). This also works as small positive constant to prevent division by zero, so should be set as 0.
L1_H	Parameter for L1 regularization (Default: 1e-10). This also works as small positive constant to prevent division by zero, so should be set as 0.
L2_W	Parameter for L2 regularization (Default: 1e-10).
L2_H	Parameter for L2 regularization (Default: 1e-10).
J	Number of low-dimension ($J < N, M_k$).
w	Weight vector (Default: NULL)
algorithm	Divergence between X and X_{bar} . "Frobenius", "KL", and "IS" are available (Default: "KL").
p	The parameter of Probabilistic Latent Tensor Factorization (p=0: Frobenius, p=1: KL, p=2: IS)
thr	When error change rate is lower than thr, the iteration is terminated (Default: 1E-10).
num.iter	The number of iteration step (Default: 100).
viz	If viz == TRUE, internal reconstructed matrix can be visualized.
figdir	the directory for saving the figure, when viz == TRUE.
verbose	If verbose == TRUE, Error change rate is generated in console window.

Value

W : A matrix which has N-rows and J-columns ($J < N, M_k$). H : A list which has multiple elements containing M_k -rows and J-columns matrix ($J < N, M_k$). RecError : The reconstruction error between data matrix and reconstructed matrix from W and H. TrainRecError : The reconstruction error calculated by training set (observed values specified by M). TestRecError : The reconstruction error calculated by test set (missing values specified by M). RelChange : The relative change of the error.

Author(s)

Koki Tsuyuzaki

References

- Liviu Badea, (2008) Extracting Gene Expression Profiles Common to Colon and Pancreatic Adenocarcinoma using Simultaneous nonnegative matrix factorization. *Pacific Symposium on Biocomputing* 13:279-290
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- Y. Kenan Yilmaz et al., (2010) Probabilistic Latent Tensor Factorization, *International Conference on Latent Variable Analysis and Signal Separation* 346-353
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Examples

```
matdata <- toyModel(model = "siNMF_Easy")
out <- siNMF(matdata, J=2, num.iter=2)
```

toyModel

Toy model data for using NMF, NTF, and NTD

Description

The data is used for confirming the algorithm are properly working.

Usage

```
toyModel(model = "CP", seeds=123)
```

Arguments

- model Single character string is specified. "NMF", "CP", and "Tucker" are available (Default: "CP").
- seeds Random number for setting set.seeds in the function (Default: 123).

Value

If model is specified as "NMF", a matrix is generated. Otherwise, a tensor is generated.

Author(s)

Koki Tsuyuzaki

See Also

[NMF](#), [NTF](#), [NTD](#)

Examples

```
matdata <- toyModel(model = "NMF", seeds=123)
tensordata1 <- toyModel(model = "CP", seeds=123)
tensordata2 <- toyModel(model = "Tucker", seeds=123)
```

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